# Crystal Structure of Methyl 3,6-Anhydro- $\alpha$-D-galactoside 

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#### Abstract

The crystal structure of the title compound has been determined using three dimensional $X$-ray diffraction data. The structure was solved by direct methods. The positional and anisotropic thermal parameters were refined using a full matrix least squares procedure to give an $R$ factor of 0.097 for 1926 reflections. Standard deviations were $\pm 0.004 \AA$ in the bond lengths and $\pm 0.2^{\circ}$ in the bond angles. The geometry of the molecule is compared with that of other monosaccharide structures and the effect of the 3,6 -anhydro-bridge is discussed. Crystal data: orthorhombic space group $P 2_{1} 2_{1} 2_{1}, Z=4, a=9.46 \pm 0.01, b=12.05 \pm 0.01, c=6.93 \pm 0.015 \AA$.


The reactions of methyl 3,6 -anhydro- $\alpha$-D-galactoside, (I), have been studied by Haworth et al. ${ }^{1}$ Two reactions clearly indicate the presence of strain within the

molecule, caused by the formation of the 3,6 -anhydrobridge, both by the products of the reactions and by the readiness with which the reactions take place. First, hydrolysis with $0 \cdot 1 \mathrm{~N}$-sulphuric acid at room temperature gives 3,6-anhydrogalactose, the properties of which indicate that it has an aldehydic structure rather than the usual hemiacetal, i.e. that the pyranose ring has been opened and second, treatment with excess of $0.5 \%$ methanolic hydrogen chloride at room temperature again causes opening of the pyranose ring with the formation of the dimethyl acetal. The presence of strain within the dicyclic system influences the method of preparation of angal as the pyranose ring must be stabilised as the methyl glycoside before the 3,6 -an-hydro-ring is formed.

The structure of (I) was determined in order to obtain a set of co-ordinates for calculations on the conformation of the polysaccharide $t$-carrageenan. ${ }^{2}$

## EXPERIMENTAL

Crystal Data. $-\mathrm{C}_{7} \mathrm{H}_{12} \mathrm{O}_{5}, M=176 \cdot 3$. Orthorhombic, $a=$ $9.46 \pm 0.01, b=12.05 \pm 0.01, c=6.93 \pm 0.015 \AA, U=$ $790 \cdot 1 \AA^{3}, \quad D_{\mathrm{m}}=1 \cdot 48, Z=4, D_{\mathrm{c}}=1 \cdot 482$. Space group $P 2_{1} 2_{1} 2_{1}, \mu\left(\mathrm{Mo}-K_{\alpha}\right)=1.37 \mathrm{~cm}^{-1}$.
(I) was prepared as previously described ${ }^{1}$ and recrystallised $(\times 3)$ as needles of rectangular or six-sided cross section. The structure was solved and the initial refinement carried out with intensity data ( 746 reflections) measured from equi-inclination Weissenberg photographs taken by use of $\mathrm{Cu}-K_{\alpha}$ radiation $(\lambda=1 \cdot 5418 \AA)$. Further refinement was carried out with intensity data (1926 reflections) collected (in collaboration with Dr. H. C. Watson, in the Biochemistry Department, University of

[^0]Bristol) on a Hilger and Watts four-circle diffractometer with Mo- $K_{\alpha}$ radiation ( $\lambda=0.7107 \AA$ ).

Solution of the Structure.-The structure was solved by the symbolic addition procedure and tangent formula refinement of phases for non-centrosymmetric space groups as described by Karle and Karle. ${ }^{3-5}$ Sixty phases of reflections with $|E| \geqslant 1.5$ were found in terms of a single unknown symbol $c$ of value $\pm \pi / 2$. The set of phases with $c=+\pi / 2$ was refined, expanded to 136 phases for reflections with $|E| \geqslant 1.18$ and again refined by use of the tangent formula. A three-dimensional $E$ map was computed with the 136 phases and structure factors were calculated for a seven-atom partial trial structure based on this map. A set of 52 calculated phases, for reflections with $|E| \geqslant 1.5$ and with $\left|F_{\mathrm{c}}\right| \geqslant 0.4\left|F_{\mathrm{o}}\right|$, was refined and expanded to a set of 145 phases $(|E| \geqslant 1 \cdot 17)$ by use of the tangent formula. A three-dimensional $E$ map calculated from these phases gave the positions of three more atoms. A Fourier synthesis was calculated including terms for which $\left|F_{\mathrm{c}}\right| \geqslant 0 \cdot 4\left|F_{0}\right|$ and the positions of the remaining two non-hydrogen atoms were easily identified.

Refinement of the Structure.-Isotropic full-matrix leastsquares refinement, based on the film data, gave $R 0.157$ for 730 reflections. A difference-Fourier synthesis showed the positions of the hydrogen atoms on $\mathrm{C}(1)-(6)$. Chemically sensible positions were calculated for the hydrogen atoms on $\mathrm{C}(1)$-(6) and on $\mathrm{O}(2)$ and $\mathrm{O}(4)$ and the contributions of these atoms to $F_{c}$ were included. They were assigned isotropic thermal parameters equal to those of the atoms to which they were attached. No attempt was made to refine the hydrogen atom parameters. Further refinement was done by use of the diffractometer data. Anisotropic thermal parameters and positional parameters of the carbon and oxygen atoms were refined in separate least-squares cycles until convergence had been achieved. The final $R$ was 0.097 ( 1926 reflections). The structural parameters together with their estimated standard deviations are listed in Tables 1-3. A diagram of the crystal structure is shown in the Figure.

Observed and calculated structure factors are listed in Supplementary Publication No. SUP 20459 (14 pp., l microfiche).*

## discussion

The geometry of the five-membered ring of (I) $[\mathrm{C}(3)-(6), \mathrm{O}(2)]$ is similar to that found in furanose rings and that of the rest of the molecule is typical of a

[^1]Table l
Atomic co-ordinates (as fractions of the cell edge) and isotropic temperature factors assigned to the hydrogen atoms, with standard deviations in parentheses

| Atom | $x$ | $y$ | $z$ | $B / \AA^{2}$ |
| :---: | :---: | :---: | :---: | :---: |
| C(1) | 0.4159(3) | 0.2103(2) | -0.0396(4) |  |
| $\mathrm{C}(2)$ | $0 \cdot 4347(3)$ | $0 \cdot 3364(2)$ | -0.0249(4) |  |
| $\mathrm{C}(3)$ | $0 \cdot 4411(3)$ | $0 \cdot 3853(2)$ | -0.2291(4) |  |
| $\mathrm{C}(4)$ | $0 \cdot 3042(3)$ | $0 \cdot 3565(2)$ | -0.3371(3) |  |
| C(5) | $0 \cdot 3344(3)$ | $0 \cdot 2335(2)$ | -0.3697(4) |  |
| C(6) | $0 \cdot 4880$ (3) | $0 \cdot 2358$ (3) | $-0.4331(4)$ |  |
| C(7) | $0 \cdot 3635(4)$ | $0 \cdot 0529$ (2) | $0 \cdot 1560$ (5) |  |
| $\mathrm{O}(1)$ | $0 \cdot 3650(3)$ | $0 \cdot 1728(2)$ | $0 \cdot 1342$ (3) |  |
| $\mathrm{O}(2)$ | $0 \cdot 3185(3)$ | $0 \cdot 3879(2)$ | $0 \cdot 0727(3)$ |  |
| $\mathrm{O}(3)$ | $0 \cdot 5502(2)$ | $0 \cdot 3297(2)$ | $0 \cdot 3339(3)$ |  |
| $\mathrm{O}(4)$ | $0 \cdot 2973$ (2) | $0 \cdot 4101(2)$ | $-0.5196(3)$ |  |
| $\mathrm{O}(5)$ | 0.3145(2) | 0.1782(1) | $-0 \cdot 1860(3)$ |  |
| $\mathrm{H}(1)$ | 0.5073 | $0 \cdot 1676$ | $-0.0673$ | $2 \cdot 73$ |
| $\mathrm{H}(2)$ | $0 \cdot 5354$ | $0 \cdot 3553$ | 0.0497 | $2 \cdot 87$ |
| $\mathrm{H}(3)$ | $0 \cdot 4637$ | $0 \cdot 4733$ | -0.2256 | $2 \cdot 56$ |
| $\mathrm{H}(4)$ | $0 \cdot 2107$ | $0 \cdot 3710$ | -0.2508 | $2 \cdot 30$ |
| $\mathrm{H}(5)$ | $0 \cdot 2678$ | $0 \cdot 1960$ | -0.4808 | $2 \cdot 23$ |
| $\mathrm{H}(6)$ | $0 \cdot 4914$ | $0 \cdot 2520$ | -0.5909 | $2 \cdot 82$ |
| H(7) | $0 \cdot 5421$ | $0 \cdot 1612$ | -0.3958 | $2 \cdot 82$ |
| $\mathrm{H}(8)$ | $0 \cdot 3250$ | $0 \cdot 3880$ | $0 \cdot 2271$ | $3 \cdot 57$ |
| $\mathrm{H}(9)$ | $0 \cdot 2750$ | $0 \cdot 5000$ | $-0.5000$ | 2.73 |

$\mathrm{H}(6)$ and $\mathrm{H}(7)$ are on $\mathrm{C}(6)$; $\mathrm{H}(8)$ is on $\mathrm{O}(2) ; \mathrm{H}(9)$ is on $\mathrm{O}(4)$.
Table 2
Anisotropic thermal parameters $\left(\times 10^{4}\right) *$ for the non-hydrogen atoms

| Atom | $\beta_{11}$ | $\beta_{22}$ | $\beta_{33}$ | $\beta_{23}$ | $\beta_{13}$ | $\beta_{12}$ |
| :--- | ---: | :--- | ---: | ---: | ---: | ---: |
| $\mathrm{C}(1)$ | 95 | 43 | 114 | 3 | -12 | -2 |
| $\mathrm{C}(2)$ | 108 | 40 | 107 | -10 | -19 | 1 |
| $\mathrm{C}(3)$ | 98 | 46 | 110 | -1 | -19 | -15 |
| $\mathrm{C}(4)$ | 90 | 38 | 87 | 2 | 2 | 7 |
| $\mathrm{C}(5)$ | 78 | 43 | 103 | -5 | -9 | -1 |
| $\mathrm{C}(6)$ | 100 | 69 | 121 | -14 | 4 | 19 |
| $\mathrm{C}(7)$ | 189 | 36 | 187 | 23 | 17 | 5 |
| $\mathrm{O}(1)$ | 156 | 49 | 107 | 6 | 28 | 12 |
| $\mathrm{O}(2)$ | 183 | 52 | 98 | 2 | 7 | 36 |
| $\mathrm{O}(3)$ | 70 | 80 | 161 | 3 | -7 | 7 |
| $\mathrm{O}(4)$ | 127 | 53 | 91 | 7 | -11 | 21 |
| $\mathrm{O}(5)$ | 110 | 39 | 129 | 7 | -19 | -11 |
| * Defined by the expression $\exp -\left(h^{2} \beta_{11}+k^{2} \beta_{22}+l^{2} \beta_{33}+\right.$ |  |  |  |  |  |  |
| $\left.2 k l \beta_{23}+2 h l \beta_{13}+2 h k \beta_{12}\right)$. |  |  |  |  |  |  |

Table 3
Bond lengths and angles for non-hydrogen atoms
(a) Bond lengths ( $\AA$ )

| $\mathrm{C}(1)-\mathrm{C}(2)$ | $1.533(3)$ | $\mathrm{C}(2)-\mathrm{O}(2)$ | $1.432(4)$ |
| :--- | :--- | :--- | :--- |
| $\mathrm{C}(2)-\mathrm{C}(3)$ | $1.534(4)$ | $\mathrm{C}(3)-\mathrm{O}(3)$ | $1.429(3)$ |
| $\mathrm{C}(3)-\mathrm{C}(4)$ | $1.535(4)$ | $\mathrm{C}(4)-\mathrm{O}(4)$ | $1.422(3)$ |
| $\mathrm{C}(4)-\mathrm{C}(5)$ | $1.526(3)$ | $\mathrm{C}(5)-\mathrm{O}(5)$ | $1 \cdot 449(3)$ |
| $\mathrm{C}(5)-\mathrm{C}(6)$ | $1.518(4)$ | $\mathrm{C}(6)-\mathrm{O}(3)$ | $1.449(4)$ |
| $\mathrm{C}(1)-\mathrm{O}(5)$ | $1.449(3)$ | $\mathrm{C}(7)-\mathrm{O}(1)$ | $1 \cdot 453(3)$ |
| $\mathrm{C}(1)-\mathrm{O}(1)$ | $1.374(4)$ |  |  |

(b) Bond angles (deg.)

| $\mathrm{C}(2)-\mathrm{C}(1)-\mathrm{O}(5)$ | $112 \cdot 8(2)$ | $\mathrm{C}(3)-\mathrm{C}(4)-\mathrm{O}(4)$ | $111 \cdot 7(2)$ |
| :--- | :--- | :--- | :--- |
| $\mathrm{C}(2)-\mathrm{C}(1)-\mathrm{O}(1)$ | $108 \cdot 0(2)$ | $\mathrm{C}(5)-\mathrm{C}(4)-\mathrm{O}(4)$ | $108 \cdot 5(2)$ |
| $\mathrm{O}(5)-\mathrm{C}(1)-\mathrm{O}(1)$ | $107 \cdot 1(2)$ | $\mathrm{C}(4)-\mathrm{C}(5)-\mathrm{O}(5)$ | $107 \cdot 0(2)$ |
| $\mathrm{C}(1)-\mathrm{C}(2)-\mathrm{C}(3)$ | $108 \cdot 9(2)$ | $\mathrm{C}(4)-\mathrm{C}(5)-\mathrm{C}(6)$ | $101 \cdot 8(2)$ |
| $\mathrm{C}(1)-\mathrm{C}(2)-\mathrm{O}(2)$ | $111 \cdot 9(2)$ | $\mathrm{O}(5)-\mathrm{C}(5)-\mathrm{C}(6)$ | $112 \cdot 8(2)$ |
| $\mathrm{C}(3)-\mathrm{C}(2)-\mathrm{O}(2)$ | $107 \cdot 4(2)$ | $\mathrm{C}(5)-\mathrm{C}(6)-\mathrm{O}(3)$ | $105 \cdot 4(2)$ |
| $\mathrm{C}(2)-\mathrm{C}(3)-\mathrm{C}(4)$ | $109 \cdot 3(2)$ | $\mathrm{C}(7)-\mathrm{O}(1)-\mathrm{C}(1)$ | $114 \cdot 9(2)$ |
| $\mathrm{C}(2)-\mathrm{C}(3)-\mathrm{O}(3)$ | $108 \cdot 5(2)$ | $\mathrm{C}(3)-\mathrm{O}(3)-\mathrm{C}(6)$ | $108 \cdot 3(2)$ |
| $\mathrm{C}(4)-\mathrm{C}(3)-\mathrm{O}(3)$ | $104 \cdot 8(2)$ | $\mathrm{C}(1)-\mathrm{O}(5)-\mathrm{C}(5)$ | $114 \cdot 0(2)$ |
| $\mathrm{C}(3)-\mathrm{C}(4)-\mathrm{C}(5)$ | $97 \cdot 7(2)$ |  |  |

[^2]pyranose sugar. ${ }^{6-10}$ Apart from $C(1)-O(1)$ the bond lengths do not differ significantly from the expected values. $\mathrm{C}(1)-\mathrm{O}(1), 1.374 \AA$, is $0.067 \AA(>18 \sigma)$ shorter than the average $\mathrm{C}-\mathrm{O}$ bond length. There is no significant asymmetry in the lengths of the $\mathrm{C}-\mathrm{O}(5)$ bonds. These two observations are in accordance with the empirical rules concerning the glycosidic bond as suggested by Chu and Jeffrey. ${ }^{7}$ The bond angles, also, have typical values though the angle $\mathrm{C}(3)-\mathrm{C}(4)-\mathrm{C}(5)\left(97 \cdot 7^{\circ}\right)$ is rather smaller than average.

The distance across the pyranose ring from $\mathrm{C}(3)$ to $C(5)$ is $2 \cdot 30 \AA$ which is $0.2 \AA$ less than that found for an unbridged pyranose ring. The distances of the four atoms $\mathrm{C}(2), \mathrm{C}(3), \mathrm{C}(5)$, and $\mathrm{O}(5)$ from their best plane


The crystal structure of (I), (100) projection, showing the packing of the molecules within the unit cell and the hydrogen bonds; hydrogen atoms are omitted
are $0.015,0.017,0.018$, and $0.012 \AA . \mathrm{C}(1)$ and $C(4)$ are 0.543 and $0.921 \AA$ out of the plane while the mean distance out of the plane for $\mathrm{C}(1)$ and $\mathrm{C}(4)$ of a glucopyranose residue is ca. $0.66 \AA .{ }^{11} \mathrm{C}(4)$ of (I) is forced further out of the plane by the formation of the $3,6-\mathrm{an}-$ hydro-bridge. On the other hand, the pyranose ring is slightly flattened at $\mathrm{C}(\mathbf{1})$. This flattening could relieve two sources of strain: first, a tendency for $O(5)$ and $C(2)$ to be pushed apart when the anhydroring is formed, and second, to relieve a rather short contact distance between $\mathrm{H}(1)$ and $\mathrm{H}(7)$ (distance between calculated hydrogen atom positions is $2 \cdot 3 \AA$ ). $C(3), O(3), C(6)$, and $C(5)$ were $0.015,0.018,0.023$, and $0.014 \AA$ out of their best plane and $C(4)$ was $0.706 \AA$ from this plane.

The position of the methyl group is also of interest. It is close to the position of the potential-energy minimum for non-bonded interactions as calculated by use of the Kitaygorodsky potential-energy function. ${ }^{12}$ The position can also be explained in terms of dipole interactions between the unshared electron pairs on $O(1)$ and $O(5)$ and is consistent with the position of the
${ }^{9}$ M. Sundaralingam, J. Amer. Chem. Soc., 1965, 87, 599.
10 C. J. Brown, Sir Gordon Cox, and F. S. Llewellyn, J. Chem. Soc., 1966, 922.
${ }^{11}$ G. N. Ramachandran, C. Ramakrishnan, and V. Sasisekharan, in ' Aspects of Protein Structure,'ed. G. N. Ramachandran, Academic Press, New York, 1963.

12 A. I. Kitaygorodsky, Tetrahedron, 1961, 14, 230.
methyl group in other similar monosaccharides. ${ }^{13}$ The dihedral angle in (I), $\mathrm{O}(5)-\mathrm{C}(1)-\mathrm{O}(1)-\mathrm{C}(7)$, is $68 \cdot 1$ compared with $72 \cdot 3,69 \cdot 2$, and $64 \cdot 8^{\circ}$ for the methyl glycosides of $\beta$-xylose, ${ }^{10} \beta$-maltose, ${ }^{7}$ and 1 -thio- $\beta$-Dxylose. ${ }^{14}$

There are two hydrogen bonds, $O(2) \cdots O\left(4^{1}\right)$ and $\mathrm{O}(2) \cdots \mathrm{O}\left(4^{\mathrm{II}}\right), \dagger 2 \cdot 845$ and $2 \cdot 744 \AA$, making double chains of molecules parallel to the $c$ axis. As in other
$\dagger$ Molecule I is at $x, y, z-1$; molecule II is at $\frac{1}{2}-x, 1-y$, $z-\frac{1}{2}$.
${ }^{13}$ A. J. de Hoog, H. R. Buys, C. Altona, and E. Havinga, Tetrahedron, 1969, 25, 3365 .
methyl glycosides there are no hydrogen bonds involving $O(5){ }^{15}$

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14 A. McL. Mathieson and B. J. Poppleton, Acta Cryst., 1966, 21, 72.
${ }_{15}$ M. Sundaralingam, Biopolymers, 1968, 6, 189.


[^0]:    * For details see Notice to Authors No. 7 in J. Chem. Soc. (A), 1970, Issue No. 20.
    ${ }^{1}$ W. N. Haworth, J. Jackson, and F. Smith, J. Chem. Soc., 1940, 620.

[^1]:    ${ }^{2}$ N. S. Anderson, J. W. Campbell, M. M. Harding, D. A. Rees, and J. W. B. Samuel, J. Mol. Biol., 1969, 45, 85.
    ${ }^{3}$ J. Karle and I. L. Karle, Acta Cryst., 1966, 21, 849.
    ${ }^{4}$ I. L. Karle and J. Karle, Acta Cryst., 1964, 17, 835.
    5 J. Karle, Acta Cryst., 1968, B, 24, 182.

[^2]:    ${ }^{6}$ G. A. Jeffrey and R. D. Rosenstein, Adv. Carbohydrate Chem., 1964, 19, 7.
    ${ }^{7}$ S. S. C. Chu and G. A. Jeffrey, Acta Cryst., 1967, 23, 1038.
    8 H. M. Berman, S. S. C. Chu, and G. A. Jeffrey, Science, 1967, 157, 1576.

